

## Estimating of CP-Violation in $B^0 \rightarrow \psi(2S)\pi^0$ Decay<sup>1</sup>

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**Abstract**—I present estimates of CP-violating asymmetries in the non-leptonic charmonium two-body  $B^0 \rightarrow \psi(2S)\pi^0$  decay and the same decays of  $B^+ \rightarrow \psi(2S)\pi^+$ ,  $B^0 \rightarrow \psi(2S)K^0$  and  $B^+ \rightarrow \psi(2S)K^+$ . These estimates are based on QCD and improved QCD factorization approach making use of next-to-leading order (NLO) contributions. The CP-violating asymmetry for  $B^0 \rightarrow \psi(2S)\pi^0$  decay is not available, according to the same calculations, it is expected if it can be measured in the future its value will be  $S_{\psi(2S)\pi^0}(B^0 \rightarrow \psi(2S)\pi^0) = 0.662 \pm 0.197$  and  $C_{\psi(2S)\pi^0}(B^0 \rightarrow \psi(2S)\pi^0) = 0.024 \pm 0.007$ .

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### 1. INTRODUCTION

$B$  meson decays to two-body final states containing a charmonium resonance such as a  $\psi(2S)$  offer a powerful way of studying electroweak transitions. Such decays probe charmonium properties and play a role in the study of CP violation and mixing in the neutral  $B$  system. Recently the Belle collaboration have reported a measurement of the  $B^0 \rightarrow \psi(2S)\pi^0$  branching fraction based on the full  $\gamma(4S)$  data set of  $772 \times 10^6 B\bar{B}$  pairs collected by the Belle detector at the KEKB asymmetric-energy  $e^+e^-$  collider [1]. From the fit to the data containing 1090  $B^0 \rightarrow \psi(2S)\pi^0$  candidates, they have obtained the bias-corrected branching fraction

$$\begin{aligned} Br(B^0 \rightarrow \psi(2S)\pi^0) \\ = (1.17 \pm 0.17(\text{stat}) \pm 0.08(\text{syst})) \times 10^{-5}. \end{aligned} \quad (1)$$

The branching fraction corresponds to 85 signal events, of which 38 are leptonic and 47 are hadronic, 628 events originate from other  $b \rightarrow (c\bar{c})q$  decays and 377 events belong to the combinatorial background. Within the factorization approach, I calculate the amplitudes for the  $B^0 \rightarrow \psi(2S)\pi^0$  decay and the same decays of  $B^+ \rightarrow \psi(2S)\pi^+$ ,  $B^0 \rightarrow \psi(2S)K^0$  and  $B^+ \rightarrow \psi(2S)K^+$  by using a color-suppressed internal W-emission and a penguin diagrams as [2]

$$\begin{aligned} A(B \rightarrow \psi(2S)M) \\ = \frac{G_F}{\sqrt{2}} \lambda_p a_i \langle \psi(2S)M | Q_i | B \rangle_F, \end{aligned} \quad (2)$$

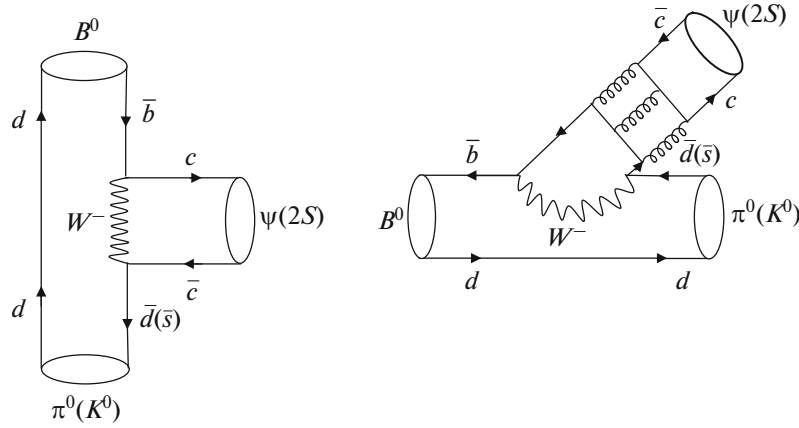
where  $M = \pi, K$ ;  $\lambda_p = V_{cb}V_{cd}^*$  ( $b \rightarrow d$  transition);  $\lambda_p = V_{cb}V_{cs}^*$  ( $b \rightarrow s$  transition);  $\lambda_p = V_{tb}V_{td}^*$  (penguin diagrams) and  $\langle \psi(2S)M | Q_i | B \rangle_F$  is the factorized hadronic matrix element, which has the same definition as that in the “nonfactorizable” approach. All the “nonfactorizable” effects (coming from the vertex-correction and hard spectator-scattering diagrams) are encoded in the coefficients  $a_i$ , which are process dependent and can be calculated perturbatively. The general form of the coefficients  $a_i$  at next-to-leading order in  $\alpha_s$ , can be written as

$$\begin{aligned} a_i(\psi(2S)M) = & \left( c_i + \frac{c_{i\pm 1}}{N_c} \right) N_i(\psi(2S)) \\ & + \frac{\alpha_s C_F}{4\pi N_c} c_{i\pm 1} (V_i(\psi(2S)) + \frac{4\pi^2}{N_c} H_i(\psi(2S)M)), \end{aligned} \quad (3)$$

where the upper (lower) signs apply when  $i$  is odd (even),  $N_i(\psi(2S))$  is the leading-order coefficient which will be considered  $N_i(\psi(2S)) = 1$ . The quantities  $V_i(\psi(2S))$  account for one-loop vertex corrections and  $H_i(\psi(2S)M)$  for hard-spectator interactions. Since the CP-violating asymmetry for  $B^0 \rightarrow \psi(2S)\pi^0$  decay is not available, the values of the  $B^+ \rightarrow \psi(2S)\pi^+$ ,  $B^0 \rightarrow \psi(2S)K^0$  and  $B^+ \rightarrow \psi(2S)K^+$  are considered for comparison with the main decay. The time-dependent CP asymmetry of neutral  $B$  decay under the improved QCD factorization are calculated at NLO scheme and different scales, they become

$$\begin{aligned} S_{\psi(2S)\pi^0}(B^0 \rightarrow \psi(2S)\pi^0) &= 0.662 \pm 0.197, \\ C_{\psi(2S)\pi^0}(B^0 \rightarrow \psi(2S)\pi^0) &= 0.024 \pm 0.007. \end{aligned} \quad (4)$$

<sup>1</sup> The article is published in the original.



**Fig. 1.** Quark diagram illustration the process  $B^0 \rightarrow \psi(2S)\pi^0$  and  $B^0 \rightarrow \psi(2S)K^0$  decays. If the spectator quarks of  $d$  to be changed with  $u$ , the decays of  $B^+ \rightarrow \psi(2S)\pi^+$  and  $B^+ \rightarrow \psi(2S)K^+$  can be obtained.

It should be noted that my calculations depend on many input parameters, among the experimental data with error bars and the theoretical values including large uncertainties. I consider the main theoretical uncertainties arising from the uncertainties of the input parameters CKM elements, the form factors and the first inverse moment of the  $B$ -meson distribution amplitude  $\lambda_B$ .

## 2. AMPLITUDE OF THE $B^0 \rightarrow \psi(2S)\pi^0$ AND $B^0 \rightarrow \psi(2S)K^0$ DECAYS

In the factorization approach, Feynman diagrams for  $B^0 \rightarrow \psi(2S)\pi^0$  and  $B^0 \rightarrow \psi(2S)K^0$  decays are shown in Fig. 1, there are a current-current and a QCD penguin amplitudes for these decay modes, it has been advocated that the new internal  $W$ -emission contribution coming from the Cabibbo allowed process  $B \rightarrow c\bar{c}d(s)$  followed by a conversion of the  $c\bar{c}$  pair into the  $\psi(2S)$  via two gluon exchanges is potentially important since its mixing angle  $V_{cb}V_{cd(s)}^*$  is as large as that of the penguin amplitude and yet its Wilson coefficient  $a_2$  is larger than that of penguin operators. In the color-suppressed internal  $W$ -emission tree ( $a_2$ ), penguin ( $a_3$ ) and electro-weak penguin ( $a_5, a_7$  and  $a_9$ ) diagrams both  $\pi^0$  and  $K^0$  mesons are placed in the form factor, the meson of  $\psi(2S)$  is produced from the vacuum state, therefore the amplitudes of these decays consist of  $\langle B^0 \rightarrow \pi^0 \rangle$  and  $\langle B^0 \rightarrow K^0 \rangle$  multiplied by  $\langle 0 \rightarrow \psi(2S) \rangle$  which are fac-

torizable terms. The form factor  $\langle P(p') | V_\mu | B(p) \rangle$  is parametrized as [3]

$$\langle M(p_M) | V_\mu | B(p_B) \rangle = \left[ (p_B + p_M)_\mu - \frac{m_B^2 - m_M^2}{q^2} q_\mu \right] \times F_1(q^2) + \frac{m_B^2 - m_M^2}{q^2} q_\mu F_0(q^2), \quad (5)$$

where  $M = \pi, K$  and  $q = p_B - p_M$ . The decay constant is defined as [4]

$$\langle 0 | V_\mu | \psi(2S) \rangle (\epsilon_{\psi(2S)} \cdot p_{\psi(2S)}) = f_{\psi(2S)} m_{\psi(2S)} \epsilon_{\psi(2S)\mu}. \quad (6)$$

Because of  $q_\mu = p_{\psi(2S)\mu}$  and  $\epsilon_{\psi(2S)\mu} \cdot p_{\psi(2S)}^\mu = 0$ , the matrix elements of the  $B^0 \rightarrow \psi(2S)M$  is given by [5]

$$\begin{aligned} \langle \psi(2S)M^0 | H_{\text{eff}} | B^0 \rangle &\propto [a_2 V_{cb} V_{cq}^* \\ &- (a_3 + a_9 + r_\chi^{\psi(2S)} (a_5 + a_7)) V_{tb} V_{tq}^*] \\ &\times f_{\psi(2S)} m_{\psi(2S)} F_1^{BM} (m_{\psi(2S)}^2) (\epsilon_{\psi(2S)} \cdot (p_B + p_M)), \end{aligned} \quad (7)$$

where  $q' = d$  for  $\pi$ ,  $q' = s$  for  $K$  mesons and

$$\begin{aligned} r_\chi^{\psi(2S)} &= \frac{2m_{\psi(2S)} f_{\psi(2S)}^\perp}{m_b f_{\psi(2S)}}, \\ \epsilon_{\psi(2S)} \cdot (p_B + p_M) &= 2\epsilon_{\psi(2S)} \cdot p_B = \frac{2m_B}{m_{\psi(2S)}} |\vec{p}|, \end{aligned} \quad (8)$$

where  $|\vec{p}|$  is the absolute value of the 3-momentum of the  $\pi$  (or the  $K$ ) in the  $B$  rest frame, and [6]

$$F_1^{BM}(q^2) = \frac{F(0)}{1 - a_F(q^2/m_B^2) + b_F(q^2/m_B^2)^2}, \quad (9)$$

$(M = K, \pi),$